Computational Image Marking on Metals via Laser Induced Heating

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Laser irradiation induces colors on some industrially important materials, such as stainless steel and titanium. It is however challenging to find marking configurations that create colorful, high-resolution images. The brute-force solution to the gamut exploration problem does not scale with the high-dimensional design space of laser marking. Moreover, there exists no color reproduction workflow capable of reproducing color images with laser marking. Here, we propose a measurement-based, data-driven performance space exploration of the color laser marking process. We formulate this exploration as a search for the Pareto optimal solutions to a multi-objective optimization and solve it using an evolutionary algorithm. The explored set of diverse colors is then utilized to mark high-quality, full-color images.

INTRODUCTION

Creating visible patterns on surfaces using laser irradiation is a rapidly growing technology with many applications in object identification, customization, and authentication [Liu et al. 2019]. Laser marking is an environmentally friendly, low maintenance process with no consumables, dyes, or pigments. While mostly a monochromatic method, some materials exhibit a range of colors when treated with laser, as a result of complex physicochemical phenomena. Among such materials are stainless steel and titanium, some of the most industrially important metals.

Despite the great potential, the industrial adoption of color laser marking is almost non-existent due to its challenging characterization. In the absence of such a characterization, the relationship
between the device’s design space (laser parameters) and performance space (e.g., marked colors) is unknown. This relationship is too complex to capture with physics-based methods [Nánai et al. 1997]. Instead, the current practice finds design parameters that lead to “interesting colors” by trial and error measurements. These primary colors are then used to mark simple motives and logos. This brute-force color gamut exploration scales poorly with the laser marking high-dimensional design space, resulting in neglecting some design parameters.

The goal of this work is to equip color laser marking with the same level of versatility found in color printers. Assuming a black-box model of the difficult device characterization, we design a measurement-based, data-driven performance space exploration. We explore different performance criteria including the color gamut and marking resolution by consecutive marking and measuring. For this, we uncover the process's Pareto front by formulating a multi-objective optimization problem and solving it using an evolutionary algorithm augmented by a Monte-Carlo approach. The optimization explores the hidden corners of our 7-dimensional design space in search of useful parameters that lead to a dense set of diverse, high-resolution colors. We also go far beyond the state of the art color image marking by introducing a complete color management workflow that takes an input image and laser-marks the closest approximation on metal surfaces. Our proposed color reproduction workflow adopts the principles of halftone-based color printing. It extracts a number of primary colors (akin to printer’s inks) from the explored gamut and reproduces input colors by juxtaposing the extracted primaries next to each other in a controlled manner. Our fabricated color images enjoy high resolution, introduce no significant artifact, and demonstrate accurate color reproduction. The main contributions of this paper are:

• A discovery algorithm that automatically finds the desired design parameters of a black-box fabrication system.

• The first color-image reproduction workflow for laser marking on metals.

2 BACKGROUND AND RELATED WORK

Color Laser Marking. The coloration of different substrates using laser irradiation is an active field of research with a long history [Birnbaum 1965]. There are many color formation mechanisms employing different laser sources and different materials; see [Liu et al. 2019] for a recent review. Surface oxidation is one of these mechanisms where the heat (generated by a laser) facilitates the reaction of materials with oxygen\(^1\). Oxidation-induced colors are believed to stem from multi-layer, heterogeneous mixture of structural colors (based on thin-film interference) [Del Pino et al. 2004] on one hand, and the traditional pigment-based color of oxides [Langlade et al. 1998] on the other hand. Despite a handful of initial efforts [Veiko et al. 2016], predicting the structure and composition of oxide layers is extremely difficult due to the complex thermodynamics of the laser marking process [Nánai et al. 1997]. Even with known material composition, predicting the surface color requires a challenging light-matter interaction model most likely based on an electromagnetic simulation [Auzinger et al. 2018]. Based on these observations, we adopt a black-box model of the process ruling out a physics-based prediction of the laser-induced composition of oxides.

For some popular metals, such as stainless steel and titanium, oxidation-based color laser marking has been extensively studied. This spans a range of laser-marked metals’ behaviors, from electromechanical [Lawrence et al. 2013] to corrosion resistance properties [LeRecka et al., 2016]. More related to our work is a class of studies focused on the effect of various process parameters on the marked colors [Laakso et al. 2009]. Most of these works [Adams et al. 2014; Antończak et al. 2013, 2014] rely on sampling and marking the process parameter space uniformly. As laser marking is time and material consuming, these methods cannot cope with the dimensions of the design space and end up ignoring a large portion of process parameters. Moreover, we are unaware of any work on exploring the marking resolution, separate or jointly by color, a critical performance criterion for high-quality image marking.

It is worth noting that some empirical color discovery methods [Veiko et al. 2016] try to find different laser parameters that lead to the same color. But that color needs to be known beforehand. Moreover, these methods are restricted to interference-based colors within a limited range of laser energy and a limited number of parameters. This work introduces the first systematic color discovery algorithm for laser marking systems.

Performance Space Exploration. In computer graphics, formulating design problems based on multi-objective optimization and solving them by computing the Pareto front is known. Notable examples are simplifying procedural shaders [Sithi-Amorn et al. 2011] or minimizing power consumption in real-time rendering [Wang et al. 2016]. In computational fabrication, exploring the performance space (or simply the gamut) of a process has attracted recent attention. With the advent of 3D additive technologies, these efforts are mainly focused on exploring the mechanical properties of 3D printed microstructures. As an example, Schumacher et al. [2015] precompute microstructures’ performance space defined by mechanical metamaterial families in order to accelerate their heterogeneous topology optimization. They first populate the performance space by perturbing the initial designs (in the design space) and then fill the unpopulated regions of the performance space through either interpolation or inverse optimization. For a similar purpose, Zhu et al. [2017] combine a discrete, random perturbation of designs near the gamut boundaries with a continuous optimization that further expands the gamut by refining existing designs. In a more general-purpose method, Schulz et al. [2018] further emphasize the importance of exploring the performance gamut’s hypersurface (or Pareto front) instead of its hypervolume. A Pareto front captures a set of solutions in the performance space that are compromising different, potentially conflicting objectives. Although these methods serve as important sources of inspiration, we cannot rely on any of them as they depend on closed-form, smooth characterization functions that connect the design and performance spaces. For example, the method of Schulz et al. [2018] requires a smooth (twice differentiable) forward characterization of the process and works only with continuous design parameters. Here, similar to Schulz et al. [2018], we cast our performance space

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\(^1\)The same phenomenon turns motorcycles’ exhaust pipes colorful.
Custom Color Reproduction. Our work is closely related to color printing as our final objective is to reproduce color images through laser marking. Color reproduction, to the best of our knowledge, is absent in the laser marking literature. The closest practice is to mark simple logos and motives without systematic reproduction in mind. Our goal is to start from a source image (e.g., sRGB) and mark its most accurate approximation on metals using a custom color reproduction workflow.

In this section, we propose a non-exhaustive performance space exploration of the laser marking system. Qualitatively speaking, our performance criteria favors diverse, saturated and high-resolution colors: the fundamental requirements for color images. Quantifying these objectives in Section 3.1, our main insight for solving this problem is to cast it as a multi-objective optimization (Section 3.2).

Unlike a typical optimization, multi-objective optimization problems are evaluated based on multiple criteria. Very often, these criteria are in conflict. In our case, for example, some marked colors may be saturated but leave thick traces and lower the resolution. Hence, instead of a single optimal solution, there exists a set of optimal solutions, known as Pareto optimal solutions or Pareto set. The projected Pareto set into the performance space is called Pareto front. A member of the Pareto front is not dominated by any other point in the performance space in all criteria. In other words, it is more performant than all other points in at least one criterion.

Our goal is to uncover a dense set of Pareto-optimal solutions to the color laser marking problem with the above objectives. To this end, we adopt a multi-objective evolutionary algorithm, a successful tool for finding Pareto optimal solutions [Fonseca et al. 1993]. The algorithm, called non-dominated sorting genetic algorithm (NSGA-II) [Deb et al. 2002] is well suited to our model-free characterization function, with both discrete and continuous parameters. At the heart of this method, is a sorting algorithm based on the members’ presence in multi-level Pareto fronts. As we show, the NSGA-II non-dominated sorting is insufficient for our specific problem due to our hue diversity objective. Thus, we resort to a Monte-Carlo approach on top of the non-dominated sorting and introduce a new sorting method based on front frequencies. We call this algorithm Monte-Carlo, multi-objective, genetic algorithm or MCMOGA for short.

3 GAMUT EXPLORATION

Device characterization is the prerequisite for any color reproduction system including laser marking. In the absence of an analytical function that maps laser marking parameters to marked colors, we must rely on data-driven methods. In a first attempt, one can sample the design space, mark and measure the sampled design points, and construct a look-up table. This exhaustive strategy is subject to the curse of dimensionality given the relatively large number (7) of parameters involved in color laser marking. The fact that function evaluations require actual marking and measuring further slows down the process. Additionally, the non-smooth color response to laser parameters renders interpolation schemes ineffective. This is shown in Figure 2 where color coordinates of marked patches may change abruptly in response to marking parameters. It is contrasted with the smooth response of a typical printer to its control parameters.

Notice the non-smooth behavior of the laser-marked colors.
The goal of our multi-objective optimization is to, eventually, maximize the following criteria:

1. **Chromacity**, as marked colors with large chroma produce more saturated color images.
   \[ f_C(a^*, b^*) = \sqrt{a^* + b^*} \]
   (1)
   where \( a^* \) and \( b^* \) are the color coordinates of the CIELAB color space [Wysecki and Stiles 1982].

2. **Hue spread** \( f_{HS} \) ensures the presence of high-chromaticity colors at all hue angles.

3. **Resolution**, since we use a line-based halftoning, this criterion is evaluated by measuring the thickness of a line marked by a set of given laser parameters.
   \[ f_R(t) = \frac{1}{t} \]
   (2)
   where \( t \) is the line thickness.

4. **Performance space diversity** \( f_{PSD} \); it is measured for each point in the CIECH space as the reciprocal of the distance to its closest two neighbors.
   \[ f_{PSD}(p, P) = \frac{1}{\arg\min_{i,j}[\|p - P_i\| + \|P - P_j\|]} \]
   (3)
   where \( p \) is the point to be scored and \( P \) its respective population in CIECH space.

5. **Design space diversity** \( f_{DSP} \); it is measured as the performance space diversity except in the design space.

Criteria (1) to (4) are measured in the performance space while criterion (5) is measured in the design space. Criteria (1) to (3) are the qualities we are directly seeking for laser marked images. Criterion (4) improves the convergence rate and criterion (5) helps avoiding local extrema by promoting solo points in the performance space.

### 3.2 Monte-Carlo Multi-objective Genetic Algorithm

Our algorithm, navigates the laser’s design space in directions that lead to a dense Pareto set, i.e., the set of designs (laser parameters) that improves the above performance criteria. We start with a random population in the design space, mark it and measure its performance, then iteratively evolve it into a larger population with as many Pareto optimal solutions as possible. At each iteration, represented schematically in Figure 3, we promote the Pareto set of its population to be passed along to the next iterations using the genetic algorithm. We stop iterating when we do not observe a significant improvement in the Pareto front.

#### 3.2.1 Monte-Carlo Multi-objective Sorting

As in almost any genetic algorithm (GA) method, a fitness measure should be assigned to each member of the population. Fitter solutions are selected by GA and used to create the next generation. Given the difficulty of assigning a single fitness value to multi-criterion objectives, the non-dominated sorting algorithm [Deb et al. 2002] sorts the members of a population according to their presence in multi-level Pareto fronts (Appendix B). It starts with finding the first non-dominated front, i.e., all solutions in a population that belong to the Pareto front. This is done by comparing each solutions’ performance objective by objective to every other solution in the population. If a solution is more performant than all other solutions in at least one criterion, it is labeled as a first-front solution. The second non-dominated front is computed by temporarily discarding the first front and repeating the above procedure. This procedure is continued until all members of the population are labeled with their respective fronts. This results in a number of disjoint subsets making up the whole population, each with its front label. Note that, in the spirit of the Pareto concept, members inside the same front are not sorted.

This type of sorting is not sufficient when considering the hue spread objective. This criterion helps the color gamut grow in all angular directions in a balanced manner. Without the hue spread criterion, the algorithm may explore some specific hue angles more than others resulting in a non-uniform growth of the chromaticity gamut. For achieving a gamut with balanced hue spread we cannot evaluate a single solution but rather in combination with other solutions. This can quickly lead to nontrivial computation: for 10 angular samples in a population of 200, we must perform \( 10^{16} \) evaluations.

We avoid this combinatorial explosion by resorting to a Monte-Carlo method. A hue wheel splits the CIECH space into a random number of circular sectors (Figure 4). Within each sector, we sort the solutions using the described non-dominated sorting algorithm based on all criteria except the hue spread. We repeat this procedure...
Once the performance space of our laser marking system is explored, it can be exploited for color image reproduction. We propose to adopt the principles of halftone-based color printing for color laser marking. For this, we find a number of primary colors (equivalent to printer’s inks) that meet our resolution requirement and produce the largest color gamut (Section 4.1). We then build a color management workflow that takes input color images and marks the closest approximation using the selected color primaries (Section 4.2).

### 4.1 Primary Extraction

The primary extraction is concerned with selecting a set of colors that generate the maximum color gamut through halftoning. While, unlike printers, the number of primaries is not strictly limited, a smaller number of primaries lead to improved marking time as they cause fewer switching delays (Section 5.1.1). Not all colors in the explored gamut can be considered for primary extraction. Thus, before primary extraction, we prune the gamut by excluding colors that: 1) don’t satisfy our specified resolution requirement, 2) reveal low repeatability, and 3) exhibit non-uniformity.

Similar to the gamut exploration, we extract the achromatic and chromatic primaries separately. We start with the explored chromaticity gamut of the laser marking system composed of a discrete set of colors. We find the convex hull of this set in the CIExy chromaticity space where

\[
X = X/(X + Y + Z), \quad Y = Y/(X + Y + Z)
\]

[Wyszecki and Stiles 1982]. The reason for applying the convex to printer’s inks]
4.2 Color Management Workflow

A color management workflow ensures color reproducibility across different imaging devices. The classic example is printing where the input images, from a camera for example, are printed as accurately as possible. Figure 5 sketches our proposed color reproduction workflow: 1. An input image is mapped to the gamut of the laser marking system. 2. In the color separation step, for each mapped color, the corresponding area coverages of each primary is computed (creating the gamut and color separation are built upon a color prediction model). 3. The continuous area-coverages are binarized and placed next to each other using a juxtaposed halftoning method. 4. The raster halftone images are converted into vectors.

Color halftoning converts a continuous tone color image into a set of binary images each corresponding to one of the printer’s inks. The discrete-line juxtaposed halftoning [Babaei and Hersch 2012] synthesizes these binary images in the form of lines and places them next to each other without overlapping.

4.2.1 Juxtaposed Halftoning. Color halftoning converts a continuous tone color image into a set of binary images each corresponding to one of the printer’s inks. The discrete-line juxtaposed halftoning [Babaei and Hersch 2012] synthesizes these binary images in the form of lines and places them next to each other without overlapping. In the original algorithm designed for bitmap printers, using digital lines [Reveilles 1995] allows for subpixel thickness, low computational complexity, and, importantly to us, continuity. A continuous laser path ensures less switching delays, and therefore, faster marking with lower graininess caused by the two ends of each marked vector. As the original juxtaposed halftoning is designed for raster devices, we need to transform the resulting raster images into vector representation suitable for our laser device. For this purpose, we use a naive line (a discrete line with unit thickness) as a mask and slide it on each halftone layer corresponding to each laser primary (Figure 5). This produces a list of vectors of different primaries which span the image plane and are sent to the laser device for marking.

4.2.2 Forward Color Prediction. The color prediction model has two roles in our proposed color management workflow. First, it constructs the color gamut generated by halftoning a set of primaries. It predicts the color of several thousands of halftones spanning the space of the relative area of primaries in each halftone, known as area coverages. The gamut surface is then fitted to this volumetric point cloud and is later used for gamut mapping. Second, the forward model is used in the color separation step that computes the area coverages of the primaries for any input colors to be reproduced.

We use the Yule-Nielsen (YN) prediction model to predict the multi-color, juxtaposed halftones of laser primaries. The Yule-Nielsen equation [Yule and Nielsen 1951] determines the CIEX color coordinate \(X_i\) of a juxtaposed halftone as

\[
X_i = \left( \sum_{j=1}^{q} a_j (X_j)^{1/n} \right)^n
\]

where \(X_i\) is the CIEX value of the \(i\)-th primary, and \(a_j\) is its area coverage. The same equation applies for predicting CIEX and CIELAB color coordinates. The exponent \(n\), called the Yule-Nielsen \(n\)-value is a tuning parameter which we further discuss in Section 5.3.

4.2.3 Color Separation. Color separation builds on the forward prediction model to compute the particular primaries and their area coverages that reproduce a given color (inside the color gamut). As the YN model is not analytically invertible, color separation is carried out by optimization:

\[
\arg \min_a \Delta d_0(\text{Lab}(YN(a)), \epsilon) \quad \|a\|_1 = 1, \quad a \in [0, 1]^q
\]

where \(\epsilon\) is the target color in the CIEXYZ color space and \(a\) is the optimization variable, i.e. the vector of area coverages of \(q\) primaries. As the CIEDE2000 color-difference formula [Sharma et al. 2005] is used for the distance metric, the modeled color using the YN model \(YN(a)\) should be converted to CIELAB from CIEXYZ (denoted by function \text{Lab} in Equation 5). Equation 5 searches for an area coverage vector that, after being marked, results in the minimum distance to the target color. As we juxtapose different primaries, their relative area coverages should sum up to 1 and be non-negative.
5 RESULTS AND ANALYSIS
In this section, we present different analyses and evaluations of both gamut exploration and image reproduction.

5.1 Experimental Setup
5.1.1 Laser Marking Hardware and Parameters. We assemble a laser marking device (Figure 6) whose main components are a ytterbium fiber laser system (IPG Photonics YLP-M-1-4x200-20-20) and a galvanometric scanner (Scanlab IntelliScan III 10). The laser system (20 W, 1064 nm) generates a laser beam which is redirected by the scanner’s Galvo Mirror system to any desired spot on the substrate. Equipped with an infrared F-Theta lens (f=163 mm), the scanner is capable of imaging a planar field of 116 × 116 mm. For safety reasons, the whole laser marking system is covered in an enclosure within which the laser source is separated by aluminum plates. An air filtering system blocks small particles from spreading in the room. In most of our experiments we use 1 mm thick stainless steel type 1.4301 V2A (AISI 304) as a substrate. We use thicker substrates and another stainless steel alloy (AISI 430) in some experiments.

In this work, we study 7 marking parameters (Figure 7), including laser parameters:

1. Frequency: Defines the number of laser shots per second (1.6-1000 kHz, 100 Hz steps),
2. Power: Adjusts the output power per shot (0-100%, 256 steps),
3. Pulse width: Defines the duration of a single shot (4, 8, 14, 20, 30, 50, 100, 200 ns),
and scanning parameters that forms a line cluster with properties:

4. Speed: Defines the travel speed along a vector while marking (0-2000 mm/s, 1 mm/s steps),
5. Line count: Defines the number of lines in a cluster (1-20 lines, 1 line steps),
6. Hatching: Defines the distance between lines within a cluster (1-15 μm, 1 μm steps),
7. Pass count: Indicates the number of times a vector is marked (1-10 passes, 1 pass steps).

5.1.2 Performance Space Measurement. For each point in the design space, we need to measure its performance in order to decide how to use that point in our exploration framework. All performance criteria, apart from the design space diversity, can be evaluated by measuring the thickness of a marked line cluster and the color of a marked patch. This is performed in two stages. First, for measuring the cluster’s thickness, we use a hand-held digital microscope (Reflecta DigiMicroscope USB 200). In a second step, we use the thickness of a given cluster to mark its corresponding patch by juxtaposing multiple clusters within the desired area.

Both hue and chromaticity, the pillars of our performance space exploration, are computed from CIELAB, a perceptual color space. We therefore perform a colorimetric calibration [Hong et al. 2001] for measuring the color of marked patches. The colorimetric calibration connects camera RGB signals to CIEXYZ coordinates through a form of regression. The CIEXYZ values then can be converted to the CIELAB coordinates using a set of well-known, analytical transformations [Wyszecki and Stiles 1982]. For training the regression, we use 121 printed color patches, with known spectra measured by an X-Rite i7 spectrophotometer, and obtain the ground-truth CIELAB color of marked patches.

We capture the same printed patches with a Nikon D750 DSLR camera (with macro lens Tamron SP 90mm F/2.8 Di) obtaining raw RGB signals that have been corrected for spatial and temporal light fluctuations. Our colorimetric calibration shows high accuracy on a test set of 16 printed patches with an average ΔE00 = 2.26 and maximum 5.00. This calibration is therefore used to estimate the CIELAB color of marked patches.

The structural nature of oxide colors causes a significant change in their appearance depending on the viewing and illumination geometry. We observe that laser-marked colors appear most saturated at specular and near-specular geometries. Therefore, inspired by previous work on metallic prints [Pjanic and Hersch 2013], we confine our color reproduction to non-diffuse geometries. To this end, the stainless steel substrate is illuminated with a large, diffuse area-light tilted approximately 45° from the substrate’s normal and captured with the camera with a similar angle.
5.2 Gamut Exploration Evaluation

For evaluating the proposed gamut exploration algorithm, we perform multiple runs while discarding different objectives during different runs to show the objective’s effect on the exploration behaviour. For a fair comparison, we always start with the same randomly generated initial population. All generations have the same population size of 100. For the hue wheel, we limit the random number of circular sections between 4 and 72 while the random angular offset $\alpha$ is between 0 and $2\pi$. The stopping threshold for MCMOS is set to 0.001%.

Figure 8 demonstrates the evolution of our chromatic gamut, in hue-chroma polar diagram, when optimizing all performance criteria (referred to as the full exploration). Overall, we see a decent evolution of colors with a symmetric, dense color gamut. Interestingly, the purple to red regions are populated with a considerable delay, suggesting that some colors are more challenging to find than others.

Comparison with Random Marking. We compare the gamut of a set of randomly marked patches (Figure 9) with the results of our exploration. Compared to our full exploration (Figure 8), random marking does not lead to adequate gamut growth. As the random exploration does not include the resolution objective, it is more illustrative to compare Figure 9d to Figure 10a as they both feature the same number of samples and none of them includes the resolution objective. The stagnant behavior of random marking over time (Figure 9) and a lack of systematic resolution enhancement suggest that a very large number of samples is required to match the full gamut generated by our algorithm.

Effect of Monte-Carlo Hue Wheel. In order to evaluate the effectiveness of our Monte-Carlo hue wheel algorithm, we run two similar explorations where the only difference is that the hue-spread objective $f_{HS}$ is enabled in one (Figure 10a) and disabled in the second (Figure 10d). We observe that the MC approach promotes the hue diversity resulting in a symmetric color gamut. Ignoring the Monte-Carlo method introduces a bias toward areas with high chromaticity. In Figure 10d, for example, since the initial population (shown in Figure 9a) has a large number of chromatic yellow members, this area is emphasized during the exploration.

Effect of Resolution Objective. Marking high-quality images requires a set of diverse, saturated colors which are placed next to each other at a high spatial resolution. This criterion is defined by $f_R$ where we encourage design parameters that mark thin line clusters. A comparison of two explorations with equal number of iterations, one with (Figure 10b) and another without (Figure 10e) the thickness minimization reveals that this objective slows down the color gamut growth and the overall gamut area by disfavoring saturated but thick colors. Crucially, however, it generates a denser gamut at lower thicknesses, visible when comparing gamuts that include only colors with small thicknesses (Figures 10c and 10f). A dense color gamut is very important during primary reproduction error of the Yule-Nielsen model for different $n$-values. (c) Extraction of chromatic primaries.
5.3 Color Image Reproduction Evaluation

We evaluate the proposed color reproduction pipeline by quantitative analysis and also a variety of full-color marked images.

**Primary Extraction.** After the pruning step discussed in Section 4.1, we obtain a total of 6 primaries including a black and white primary and 4 chromatic primaries shown in Figure 11c. Their parameters are reported in Appendix A. In the pruning stage, we check the spatial and temporal repeatability by marking the candidate primaries at four different locations of the substrate and compare their colors pairwise. Primaries having an average $\Delta E_{00}$ higher than 4 among all comparisons are discarded. Also for the progressive primary discarding, we reduce the number of primaries until the gamut area drops by more than 10%. For resolution pruning, in this work, we keep colors with thickness $40 \pm 5 \mu m$. Additionally, we consider colors with thickness around 20 $\mu m$ as juxtaposing two of them results in the target resolution.

**Prediction Model Accuracy.** For testing the accuracy of the Yule-Nielsen model, we mark the primaries and also 92 test patches with diverse area coverages of primaries. The resulting average $\Delta E_{00}$ error is 2.25 ($\text{Std}=0.96$, $\text{Min}=0.50$, $\text{Max}=4.26$) that demonstrates the high accuracy of our forward model. As we show in Figure 11b, the $n$-value equal to 1 works very well for our configuration, reducing our model to the widely known Neugebauer model [Rolleston and Balasubramanian 1993]. There are a handful of physical and empirical interpretations of the Yule-Nielsen $n$-value in literature [Lewandowski et al. 2006]. In the classic ink-on-paper prints, it accounts for the optical dot gain due to the lateral propagation of light inside the substrate [Hébert 2014]. Babaei and Hersch [2015] showed that this parameter is responsible for shadowing and masking in metallic-ink halftones. From the optimal $n$-value for our setup we can infer that, as expected, the subsurface scattering in metal is very negligible. Furthermore, the marked primaries are very well leveled on the surface and cause no shadowing or masking.

**Marking Color Images.** Figure 12 presents different results generated by the proposed image reproduction pipeline with the chosen primaries. Comparing the marked images with their gamut-mapped counterparts, we can observe that the colors are reproduced faithfully. Furthermore, no significant artifacts are introduced in the laser-marked images. The gamut of the primary set allows marking diverse, vivid and relatively saturated colors as pointed by the image in the second row of Figure 12. Thanks to the high-resolution primaries, high spatial frequencies are preserved. This allows marking images with a vast level of details as shown in the bottom-right row of Figure 12.

5.4 Repeatability and Generalizability

In this section, we study the question of whether the marking parameters are transferable when using different marking settings or substrates. We start by marking a set of parameters reported in literature [Antończak et al. 2013] and show the results in Figure 13. Despite using highly similar hardware and materials, the reported
colors are not reproducible on our setup. Also, color thicknesses vary significantly making them unsuitable for halftoning and therefore image marking.

In Table 1, we report color differences when marking on our setup a general set of parameters in different circumstances. The general set, consisting of 89 design points, is chosen to represent different colors in our explored gamut. We can see a pure repeatability test, on AISI 304 alloy, using the same marking settings leads to acceptable but not satisfactory accuracy. When we change the marking settings by using a thicker substrate (2 mm), and therefore exiting the focal plane, the repeatability worsens. Finally, using a different alloy of stainless steel (AISI 430) results in the worst repeatability.

For comparison, in Table 1, we also show the result of the same experiments performed using our 6 extracted primaries. We observe significantly higher accuracy in the pure repeatability experiment as the primaries have been pruned against this circumstance. Interestingly, the primaries show acceptable repeatability when marked out of focus indicating that the extracted primaries are robust against some perturbations. However, the larger deviation when using a new substrate suggests that the primaries cannot be used for marking images on new substrates accurately.

In Figure 14, we mark an image on a new substrate (stainless steel AISI 430) using primaries explored and extracted on our default substrate (AISI 304). While the image on the new substrate preserves the spatial details, most colors are significantly paler compared to the image marked on the default substrate. Thus, we perform a complete gamut exploration, primary extraction and color reproduction on the new substrate and show the results in Figure 14 (bottom row). Note that we cannot expect the same reproduction as on the default substrate since the color gamuts on two substrates are different. The gamut of the new substrate, calculated using a full exploration, is shown in Figure 15 (gamut obtained on the default substrate is shown in Figure 8).

Table 1. Repeatability errors of color laser marking in form of $\Delta E_{00}$ mean (and standard deviation).

<table>
<thead>
<tr>
<th>Substrate A</th>
<th>AISI 304</th>
<th>AISI 304</th>
<th>AISI 304</th>
</tr>
</thead>
<tbody>
<tr>
<td>Substrate B</td>
<td>AISI 304</td>
<td>2 mm thick AISI 304</td>
<td>AISI 430</td>
</tr>
<tr>
<td>General set</td>
<td>3.42 (3.63)</td>
<td>9.39 (6.27)</td>
<td>16.37 (15.39)</td>
</tr>
<tr>
<td>Primaries</td>
<td>1.96 (1.06)</td>
<td>6.46 (4.15)</td>
<td>12.81 (7.23)</td>
</tr>
</tbody>
</table>

5.5 Performance
An iteration of the gamut exploration with a population size of 100 takes around 30 minutes. This includes marking the single clusters, measuring their thicknesses with a handheld microscope, marking the corresponding patches with proper distances of clusters, and finally capturing them with our colorimetric camera. The manual measurement of cluster thicknesses is the bottleneck as it takes approximately 20 minutes. Computing a new generation using the MCMOGA takes only a few seconds in Matlab.

The marking time of an image is a function of the number of vectors (after halftone vectorization) and the marking speed of different primaries. A larger number of vector causes more switching delays, making the marking time highly dependent on the image content in addition to its size. For example, the two marked images in the top row, and right side of the bottom row of Figure 12, despite a comparable image size (7 by 11 cm), required around 18 and 30 million vectors, and roughly 3 and 5.5 hours of marking time, respectively.

6 Conclusion
We presented a computational framework that enables a novel application of laser marking: color image reproduction. Our method first characterizes the device using an evolutionary exploration of its performance space and then exploits that space for marking high-resolution, colorful images.
Pitfalls, Limitations and Outlook. Proper imaging was a challenging part of this research. We started the colorimetric calibration of the camera using the spectra of laser-marked patches (and not printed colors on paper). Although our spectrophotometer can perform measurements that include the specular component, the measured spectra were inconsistent with reality. Fortunately, switching to the printed colors for calibrating the colorimetric characterization proved to be robust. Another imaging-related issue was measuring the thickness of the clusters using a camera. The efforts were not successful and led to the use of a handheld microscope that significantly slowed down our exploration.

A clear limitation of our method is the significant change of appearance from diffuse to non-diffuse configurations as shown in Figure 16. While amusing, producing plausible images in a wider range of viewing/illumination geometries is an important research direction and a formidable challenge. In the future, we plan to analyze the performance of our method in the case the pruning stage is integrated into the exploration using new objectives. We intentionally did not consider the physical phenomena behind the laser marking and stayed with a black-box approach. Yet we believe a combination of both physical and data-driven methods can make the color image marking task more scalable.

A PRIMARY PARAMETERS

The design and performance space parameters of the extracted set of primaries are shown in Table 2. In the project’s website, we also publish the intermediate exploration data, i.e., design parameters and performance measurements for all marked patches at all iterations of our full exploration.

Table 2. Design and performance space parameters of extracted primaries on AISI 304 (top segment) and AISI 430 (bottom segment).

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<th>Frequency</th>
<th>Power</th>
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<th>Speed</th>
<th>Line count</th>
<th>Hatching</th>
<th>Pass count</th>
<th>CIELAB</th>
<th>Iμ, Iν, Iλ</th>
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<td>ms</td>
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REFERENCES


